NACA

RESEARCH MEMORANDUM

A PRELIMINARY INVESTIGATION OF THE USEFULNESS OF CAMBER

IN OBTAINING FAVORABLE AIRFOIL-SECTION DRAG

CHARACTERISTICS AT SUPERCRITICAL SPEEDS

By Gerald E. Nitzberg, Stewart M. Crandall,
and Perry P. Polentz

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NATIONAL ADVISORY COMMITTEE
FOR AERONAUTICS

National Aeronautics and
Space Administration

Langley Research Center
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SUMMARY

An investigation was made to determine the possibility of delaying at moderate or large lift coefficients the onset of the abrupt super-critical drag rise of an airfoil section by the use of camber. An analysis of the data from previous experimental studies, supplemented by calculations of drag—divergence characteristics of two basic thickness forms in combination with a variety of mean lines, indicates that significant gains in high—speed drag characteristics are to be obtained by cambering some airfoil sections. It was found experimentally, as predicted, that for an NACA 0010 airfoil section marked increases in drag—divergence Mach number are obtained by cambering the airfoil for a design lift coefficient of 0.3 with an NACA $a = 1.0$ mean line.

INTRODUCTION

Early attempts to design airfoil sections which were advantageous for high—speed applications were based on considerations of the critical Mach number. The critical Mach number of a cambered airfoil section is usually higher, at moderate lift coefficients, that that of the symmetri-cal basic thickness form. However, when experimental data were obtained, it was found that the addition of camber led to adverse effects on the high—speed lift and pitching—moment characteristics and, in some cases, on the drag characteristics too. Because of these unpromising results no systematic study has been made of the effects of camber on high—speed force characteristics of airfoil sections.

Reference 1 shows that the drag—divergence Mach number, the Mach number at which the abrupt supercritical drag rise begins, provides a more useful criterion than critical Mach number for the study of the effects of shape changes on airfoil—section characteristics at high speeds. This reference also suggests a method for calculating

drag—divergence Mach number.

The purpose of this investigation is to determine the possibility of increasing, at moderate or large lift coefficients, the drag—divergence Mach number of airfoil sections by the use of camber. Data of previous experimental investigations were examined and an analysis, using a method suggested by reference 1, was then made of the effect of a systematic variation of mean line on the drag—divergence Mach number of two basic thickness forms. As a result of this analysis a cambered airfoil section was designed which was expected to have higher drag—divergence Mach number at moderate lift coefficients than the basic thickness form. In order to determine whether the anticipated gains were realized and what effect this shape change had on other high—speed force characteristics, lift, drag, and pitching—moment data were obtained for the two (symmetrical and cambered) airfoil sections in the Ames 1— by 3—1/2—foot high—speed wind tunnel. These data are compared with experimental values for the NACA 64A010 air—foil section, which is generally considered to possess good high—speed characteristics.

NOTATION

a   mean—line designation, fraction of chord from leading edge over which design load is uniform

a_0 lift—curve slope, per degree

α_0 angle of attack, degrees

c   airfoil chord

c_d section drag coefficient

c_l section lift coefficient

c_{l_i} design section lift coefficient

$c_{m_c/4}$ section pitching—moment coefficient about quarter—chord point

M   free—stream Mach number

M_d drag—divergence Mach number
             (Mach number at which slope of curve of drag coefficient versus Mach number attains a value of 0.10.)

P   pressure coefficient $\left(\dfrac{p-p_0}{q_0} \right)$

p   local static pressure

p_0 free—stream static pressure

P_R resultant pressure coefficient, difference between local upper-
and lower—surface pressure coefficients

q_o free—stream dynamic pressure

x distance along chord

y distance perpendicular to chord

y_c mean—line ordinate

ANALYSIS

Analysis of Experimental Data

Plots of the drag—divergence Mach number versus lift coefficient are
presented in figure 1 for a number of cambered airfoil sections derived
from four NACA basic thickness forms. The experimental data presented in
figure 1 were obtained from references 2, 3, and 4 and include substan-
tially all the available experimental information applicable to the problem.
The calculated curves shown in this figure will be discussed later. For
the convenience of the reader the types of thickness distributions and
mean—line shapes considered throughout the report are presented in figure 2.

The values of drag—divergence Mach number presented in figure 1 were
determined as the free—stream Mach number at which the slope of the curve
of drag coefficient against Mach number for a constant angle of attack has
a value of 0.1. Ordinarily this definition provided a good measure of the
free—stream Mach number at which the drag coefficient ceased to be essen-
tially independent of Mach number and began to increase abruptly. However,
for data obtained at Reynolds numbers below about 2 million it was often
found that the increase in drag coefficient took place gradually instead
of abruptly. For such data, the concept of drag divergence occurring at a
definite Mach number has less utility, and conclusions based thereon must
be made with less assurance. Flagged symbols are used in the figures to
indicate results of this nature.

The data of figure 1 show that, except for the thin NACA 16—006 series
airfoil sections, the addition of camber had little or no beneficial effect
on the drag—divergence Mach number at moderate lift coefficients (0.2 to
0.4). In the majority of cases, however, it is to be noted that signifi-
cant gains were obtained at high lift coefficients. If this gain could be
extended to lower values of lift coefficient, it would be advantageous to
do so.

Analysis Utilizing Calculated Data

To investigate the possibility of extending the useful range of camber
to lower lift coefficients, the method suggested in reference 1 was used to

compute the effect on drag–divergence Mach number of a systematic variation
of camber. A brief review of the theory of this reference and a numerical
example illustrating the method are presented in an appendix to this report.
In studying the effect of camber on the drag–divergence Mach number, it is
important to make comparisons on the basis of equal lift coefficients rather
than equal angles of attack. This required introducing a slight variation
of the method of reference 1. Calculated values of drag–divergence Mach
number compared with experimental values in figure 1 indicate that this
calculation procedure leads to results which are in substantial agreement
with experiment.

The effects of several types of camber lines, in combination with the
NACA 0010 and 64A010 thickness distributions, on the calculated variation
of drag–divergence Mach number with lift coefficient are considered in
three categories: (1) Effects produced by different types of chordwise
distribution of camber, each with approximately the same position of maxi-
mum camber; (2) effects of marked variation of the position of maximum
camber for camber lines with equal design lift coefficients; and (3)
effects of different amounts of camber for a given type of mean line. Each
of these will be discussed in turn.

The calculated drag–divergence Mach numbers for the two airfoil sec-
tions to which have been applied the NACA a = 1.0, 65, a = 0.4, and 64–
type camber lines are presented in figure 3. As may be seen in figure 2,
the first two of these camber lines have the position of maximum camber
at 50–percent–chord station, and the latter two at 40 percent. In each
case the amount of camber corresponds to a design lift coefficient of 0.3.
The principal observation to be made from figure 3 is that, for a given
basic thickness form and a given chordwise location of the point of maxi-
mum camber, the choice of the particular camber line to be used appears
to be of some importance but is secondary to effects of other camber vari-
ations discussed later. It is also interesting to note that, although
application of camber to the NACA 64A010 basic thickness form provides no
gain at lift coefficients smaller than about 0.4, application of camber to
the NACA 0010 basic thickness form provides distinct improvement of the
drag–divergence Mach number for lift coefficients larger than about 0.1.

The effect of varying the position of maximum camber for camber lines
with design lift coefficients of 0.3 is indicated in figure 4. The mean
lines used in this comparison are the NACA 62, 65, and 68 types. It is
noted (fig. 4(a)) that the NACA 68–type camber line (maximum camber at 80–
percent chord) offers more improvement in drag–divergence Mach number than
does either the NACA 65 or 62 camber line (maximum camber at 50–percent and
20–percent chord, respectively). Figure 4(b) indicates that with rearward
shift of the position of maximum camber there is an increase in drag–
divergence Mach number at lift coefficients greater than about 0.2 and a
decrease in drag–divergence Mach number at smaller coefficients for the
NACA 0010 basic thickness form.

The effect of varying the amount of camber, for the a = 1.0 type of
camber line, is shown in figure 5 for these same two basic thickness forms.

At positive lift coefficients up to about 0.5, the figure demonstrates
that the NACA 64AX10 airfoil sections have essentially the same drag-
divergence Mach number for varying amounts of camber corresponding to
design lift coefficients ranging from 0 to 0.3. For the NACA 0010
airfoil section,large increases in the drag-divergence Mach number at
moderate and large lift coefficients are found with amounts of camber
up to that corresponding to a design lift coefficient of about 0.3.
An amount of camber greater than that corresponding to a design lift
coefficient of 0.3 leads to further gains at large lift coefficients
but to losses at small and moderate lift coefficients for both basic
thickness forms.

Comparison of data contained in figures 3, 4, and 5 pertaining just
to the NACA 64A010 profile indicates that none of the camber lines con-
sidered produced significant increases in the drag-divergence Mach number
of the NACA 64A010 airfoil section at small or moderate lift coefficients.
In contrast, a similar comparison for the NACA 0010 airfoil section indi-
cates that marked improvement in the drag-divergence Mach number charac-
teristics of this airfoil section seems to be provided by some camber lines
in common usage, such for example as the a = 1.0 mean line. It is thus
concluded that profiles exist for which the proper choice of camber may
significantly improve the high-speed drag characteristics, but that uni-
versal improvement is not to be expected.

EXPERIMENTAL INVESTIGATION

To determine to what extent the predicted gains from the use of camber
could be attained for an airfoil section considered in the preceding analysis,
tests of the NACA 0010 (reference 5) and NACA 0010, a = 1.0, $c_{l_i} = 0.3$
airfoil sections were made in the Ames 1- by 3-1/2-foot high-speed wind
tunnel. The measured section drag, lift, and pitching-moment coefficients
are presented in figure 6. The models were of 6-inch chord and the test
Reynolds number varied from 1 million to 2 million with increasing Mach
number.

Cross plots, for various constant section lift coefficients, of the
variations with Mach number of section drag coefficient, section angle of
attack, section lift-curve slope, and section pitching-moment coefficient
are presented in figures 7, 8, 9, and 10, respectively. Comparison with
similar data for the NACA 64A010 airfoil section (reference 6) is made
because this airfoil section is generally considered to have good section
characteristics at high subsonic Mach numbers and thus it provides a meas-
ure of the suitability of the cambered conventional airfoil for high-speed
applications.

Examination of figure 7 shows that the addition of camber was very
effective in improving the drag characteristics of the uncambered basic
thickness form at section lift coefficients of 0.2, 0.4, and 0.6. The
magnitude of the improvement, moreover, was enough to make the section

drag coefficients for the cambered conventional airfoil section as small
as, or smaller than, those of the symmetrical NACA 64A010 section. The
variations with Mach number for constant lift coefficient of the section
angle of attack, the section lift—curve slope, and the section pitching—
moment coefficient for the cambered NACA 0010 airfoil section (figs. 8, 9,
and 10) are all essentially similar to those of the NACA 64A010 airfoil
section throughout the range of Mach numbers for which data were obtained.

CONCLUDING REMARKS

The results of this investigation demonstrate that a proper addition
of camber to the NACA 0010 airfoil section leads to significant improve—
ments in the drag characteristics at moderately supercritical speeds. It
has been shown further that,within the test range of Mach numbers, all the
high—speed aerodynamic characteristics of this cambered airfoil section are
equivalent to those of the NACA 64A010 airfoil section, which is generally
considered to have good high—speed characteristics.

At Mach numbers above the maximum reached in these tests, it is prob—
able that the lift and pitching—moment characteristics of cambered NACA
0010 airfoil sections will undergo large variations such as are character—
istic of other cambered sections. With some cambered sections it has been
possible to reduce these variations by use of upwardly deflected plain flaps.

The preliminary analysis which has been made indicates that moderate
amounts of camber and a rearward location of the position of maximum camber
are most conducive to increasing the drag—divergence Mach number at moderate
lift coefficients. An important limitation to this working hypothesis is
that extreme rearward location of maximum camber imposes large adverse pres—
sure gradients over the rear portion of the airfoil upper surface. Such
gradients might be expected to cause boundary—layer separation and hence
poor characteristics at high speeds.

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APPENDIX

Theoretical Basis for the Calculation
of Drag—Divergence Mach Number

An analysis of the experimental pressure distributions over a number
of airfoil sections was presented in reference 1. It was found that, for
an airfoil section at a fixed angle of attack, as the free—stream Mach
number is increased past the critical Mach number, the local region of
supersonic flow over the airfoil increases in chordwise extent. However,

the abrupt supercritical drag rise does not begin until the supersonic region envelops the airfoil crest. The airfoil crest is the chordwise location at which, for a given angle of attack, the tangent to the air-foil surface lies in the free—stream direction. After the shock wave which terminates the supersonic region moves aft of the airfoil crest the pressure distribution over the forward portion of the airfoil varies in such a manner that, with further increase in free—stream Mach number, the local Mach number at each chordwise station remains essentially con-stant. Thus, pressure coefficients ahead of the crest become less nega-tive while those on the afterportion of the airfoil continue to become more negative. The resulting pressure drag is the primary cause of the abrupt supercritical drag rise. The free—stream Mach number at which this abrupt drag rise begins, the drag—divergence Mach number, is calcu-lated by determining from the low—speed pressure distribution the free-stream Mach number at which the local velocity at the airfoil crest is sonic. The significance of local sonic velocity arises from the experi-mentally observed fact that, as long as there is no extensive flow separa-tion, the terminal shock wave is located near the point on the airfoil surface at which the local pressure coefficient corresponds to sonic velocity.

Numerical Example of Procedure for Calculating the Drag—Divergence Mach Number of an Airfoil Section

In calculating the variation of drag—divergence Mach number with lift coefficient for an airfoil section, it is convenient to determine the drag—divergence Mach number and lift coefficient for which the airfoil crest is located at various standard chordwise stations. This is a consequence of the fact that the theoretical velocity distributions for airfoil thickness and camber shapes are usually tabulated at these standard stations. To illustrate the procedure for calculating drag—divergence Mach number, consider the conditions under which the crest is at the 0.20—chord station for an NACA 0010 airfoil section with an NACA $a = 1.0$ camber line having a design lift coefficient of 0.3. The thickness distribution for the NACA 0010 airfoil section is given in reference 7. From this, the slope of the symmetrical airfoil at the 0.20—chord station can be found graphically to be 0.048. Although cambered airfoils are derived by adding the thickness distribution perpendicular to the mean line, it is sufficiently accurate to determine the slope of the upper surface of the airfoil by taking the sum of the slope of the basic thickness form and the slope of the mean line. Reference 7 contains the values of the slope of the NACA $a = 1.0$ camber line at various standard stations. For a design lift coefficient c_{l_i} of 0.3 the slope at the 0.20—chord station is 0.033. Thus, for the upper surface of the cambered airfoil, the tangent to the 0.20—chord station lies in the free—stream direction when

$$\tan \alpha_o = 0.048 + 0.033 = 0.081$$

which corresponds to an angle of attack of 4.6°. Noting that for thin airfoil sections the lift—curve slope is about 0.11 and that the NACA

a = 1.0 camber line attains its design lift at zero angle of attack, it
follows that the low—speed additional lift coefficient (lift coefficient
due to angle of attack) for the case being considered is 0.51. From
reference 7, it is found that the local velocity at the 0.20—chord station
for the NACA 0010 section at an additional lift coefficient of 0.51 is
1.312 times the free—stream velocity. The velocity—ratio increment due
to the camber loading is 0.075, so the total local velocity is 1.387 times
free—stream velocity. The corresponding pressure coefficient is

$$P = 1 - (1.387)^2 = -0.92$$

In order to determine the free—stream Mach number M at which this pres—
sure coefficient corresponds to the occurrence of local sonic velocity,
it is assumed that the pressure coefficient varies with Mach number in
accordance with the Prandtl—Glauert compressibility factor. The problem
then reduces to the solution of the equation

$$\frac{P}{\sqrt{1-M^2}} = \frac{2}{1.4M^2}\left[\left(\frac{2}{2.4} + \frac{M^2}{6}\right)^{3.5} - 1\right]$$

For P equal to —0.92, M is found to be 0.62. The lift coefficient at
which 0.62 is the drag—divergence Mach number is then calculated to be 1.02
by correcting the low—speed lift coefficient, 0.81, by the compressibility
factor.

Calculations must be made for a sufficient number of chordwise stations
to define the curve of drag—divergence Mach number versus lift coefficient.
Values should be computed only for points behind about the 7—percent—chord
station because calculations made for stations nearer the leading edge of
the airfoil are usually not in satisfactory agreement with experiment.

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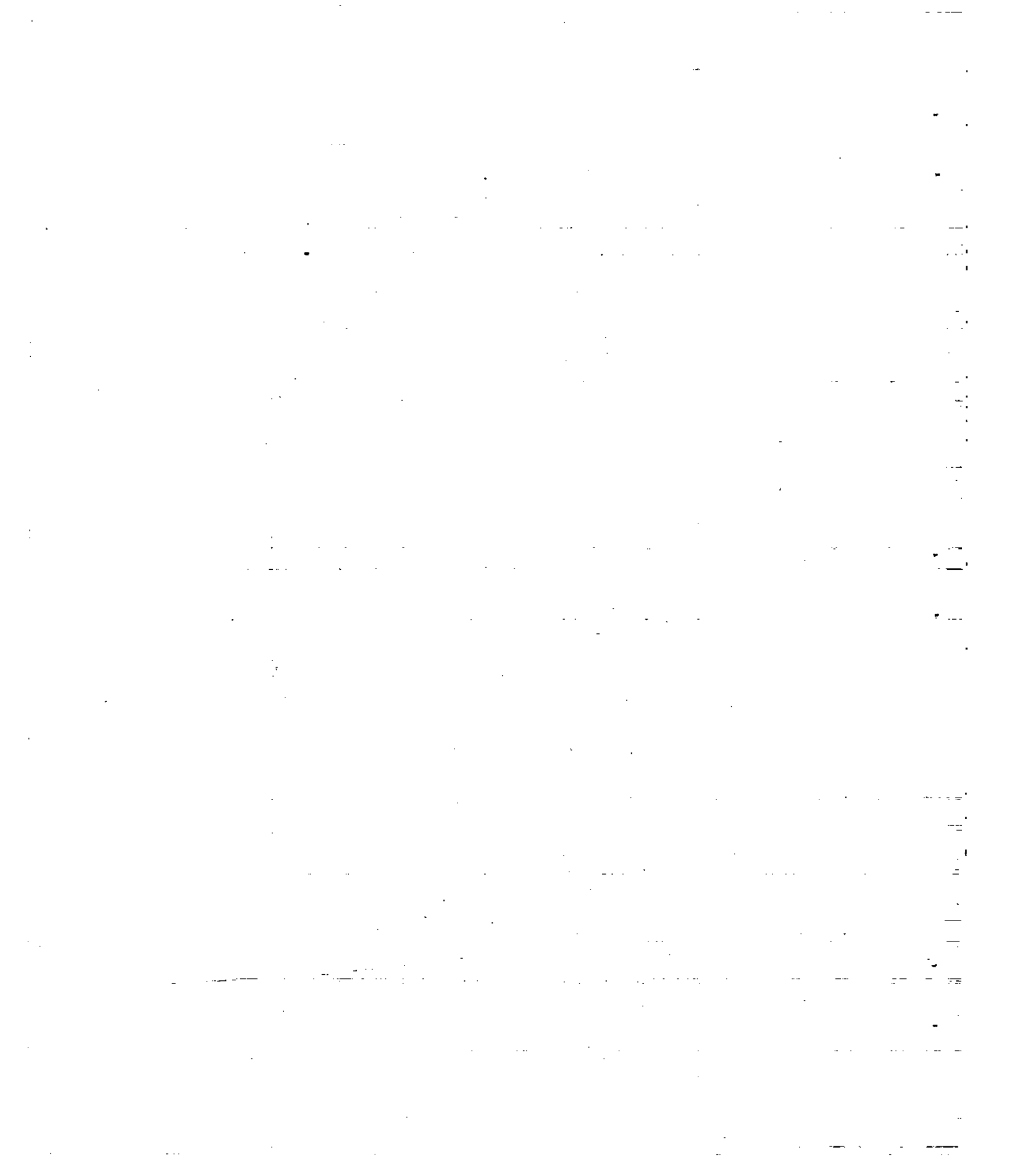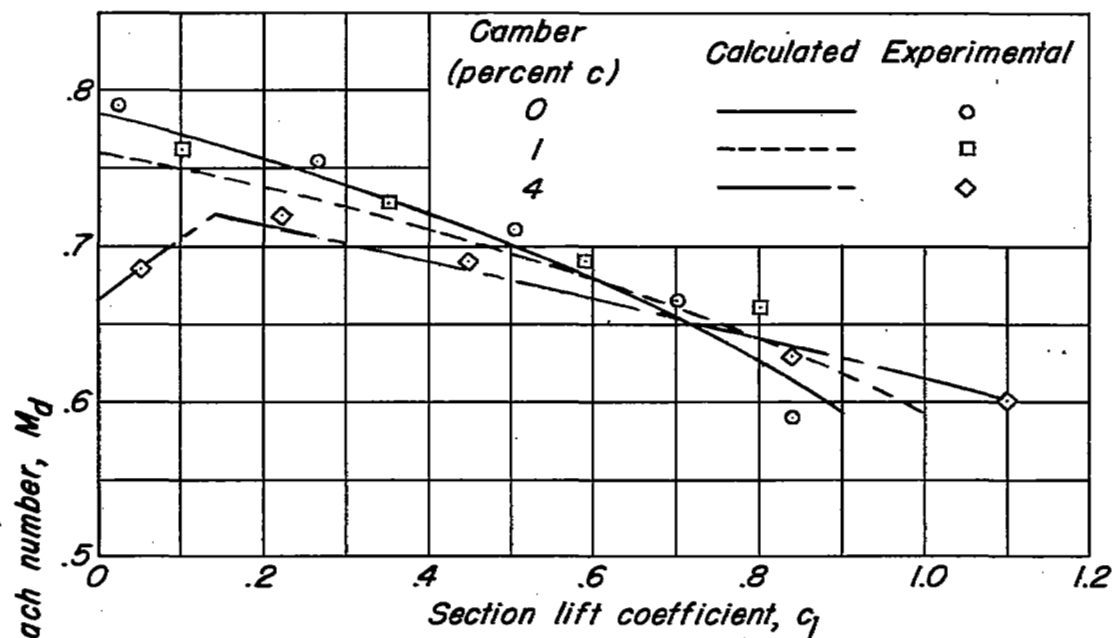
(a) Basic thickness form, NACA 0012-44; type of mean line, NACA 270. Data from reference 2.
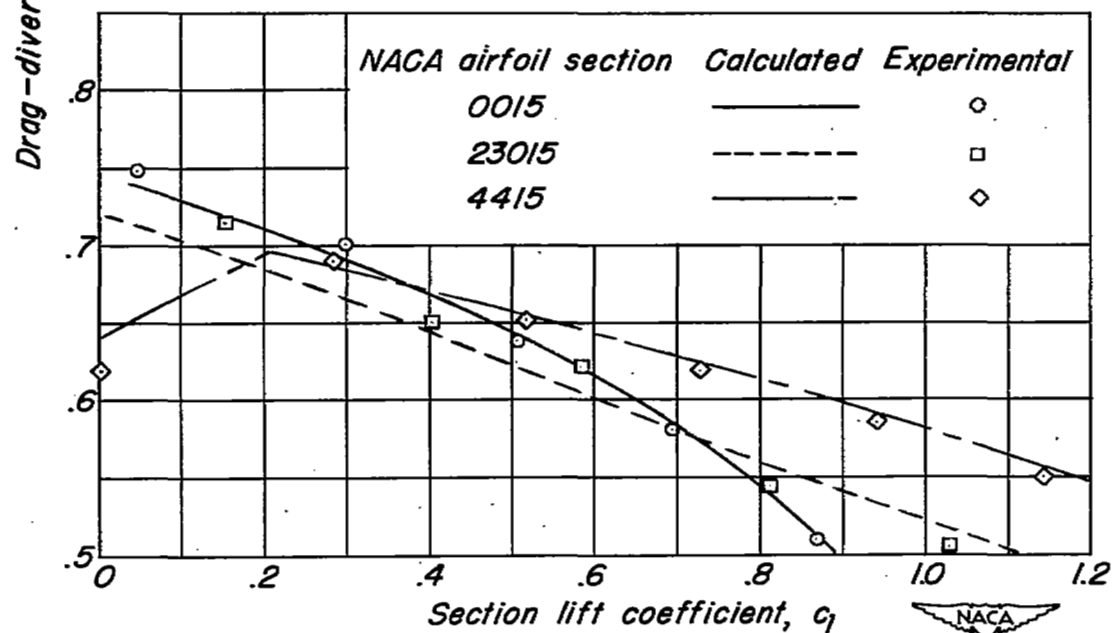
(b) Basic thickness form, NACA 0015. Data from reference 3.

Figure 1.— Effect of camber on the variation of drag—divergence Mach number with section lift coefficient for several basic thickness forms.
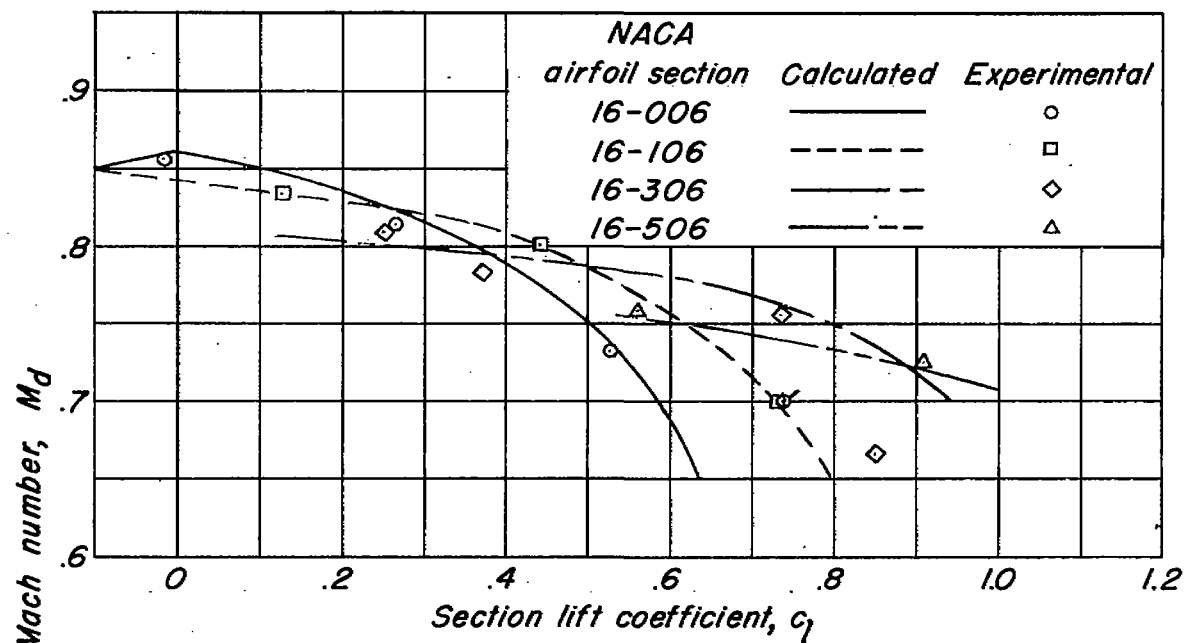
(c) Basic thickness form, 16-006. Data from reference 4.
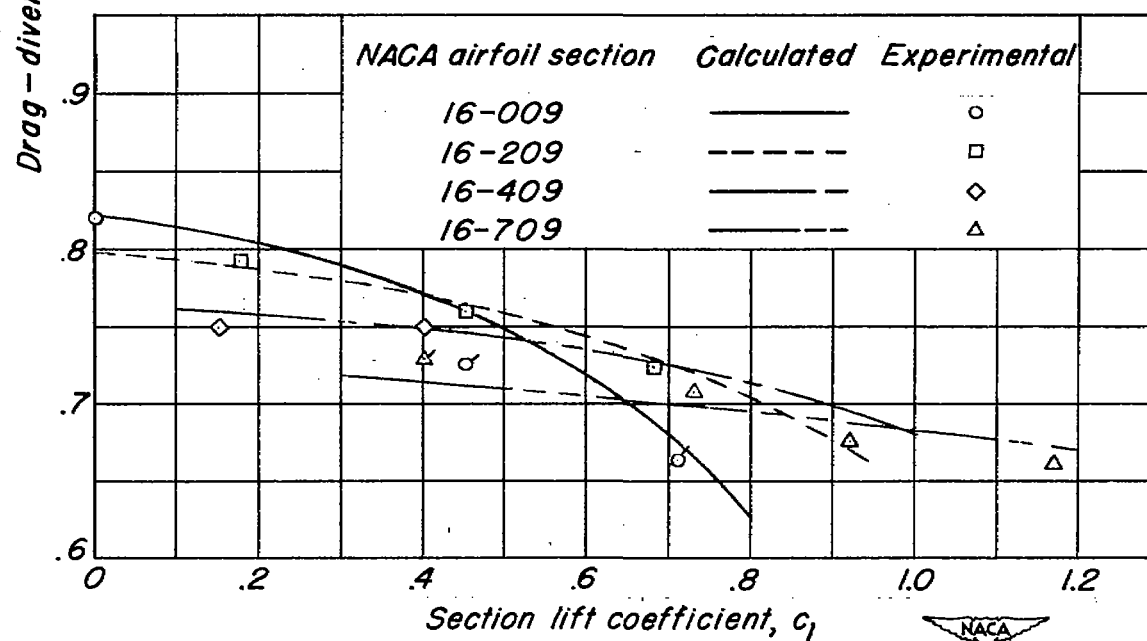
(d) Basic thickness form, 16-009. Data from reference 4.

Figure 1.—Concluded.
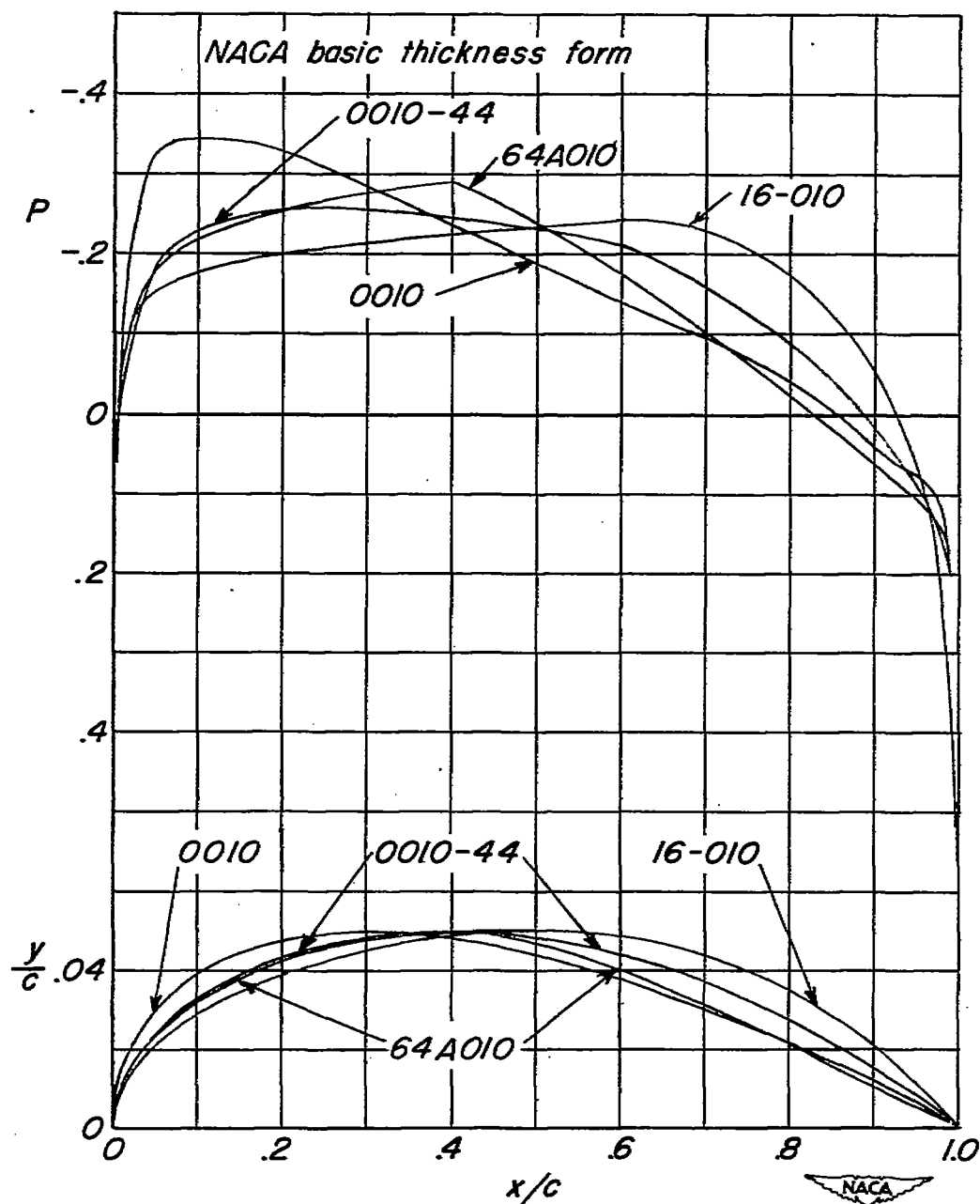
(a) Basic-thickness-form ordinates and pressure
distributions.

Figure 2.- Shapes and pressure distributions of the various
airfoil-section mean lines and thickness distributions
considered.
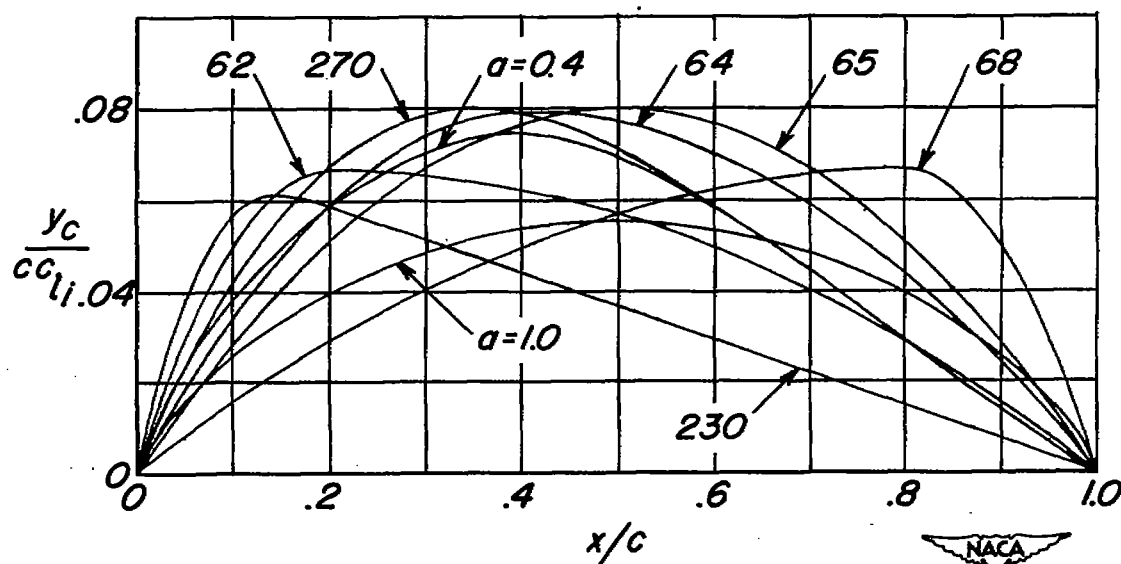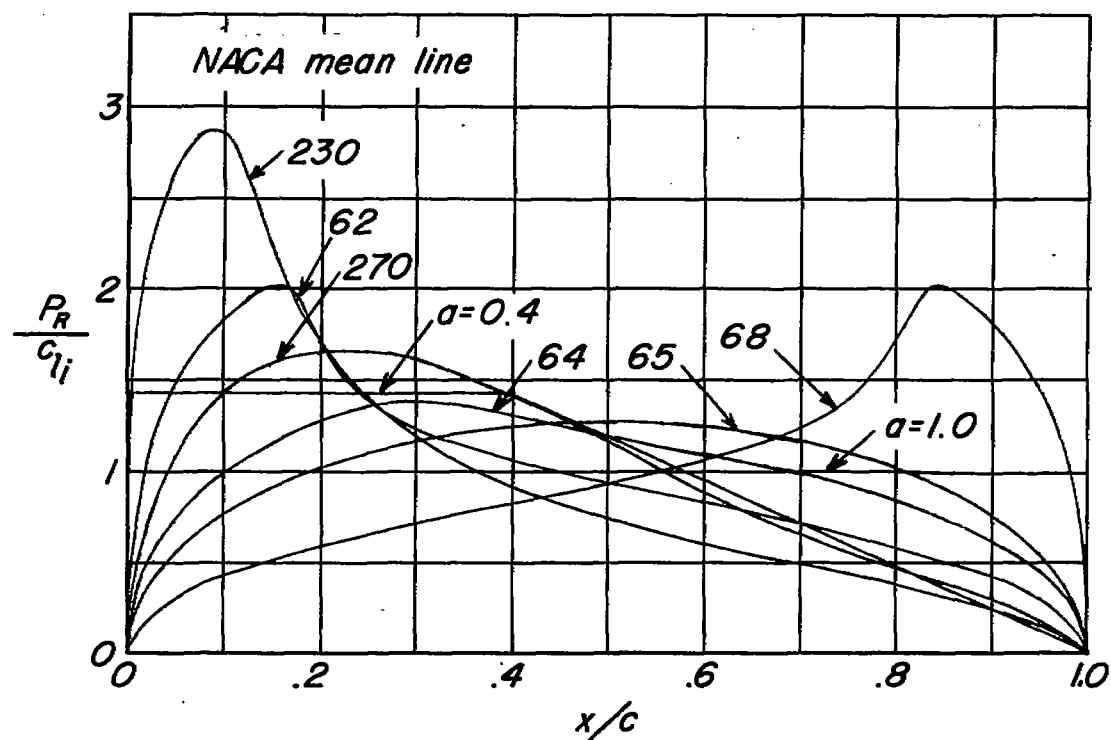
(b) Mean lines and mean—line load distributions.

Figure 2.—Concluded.
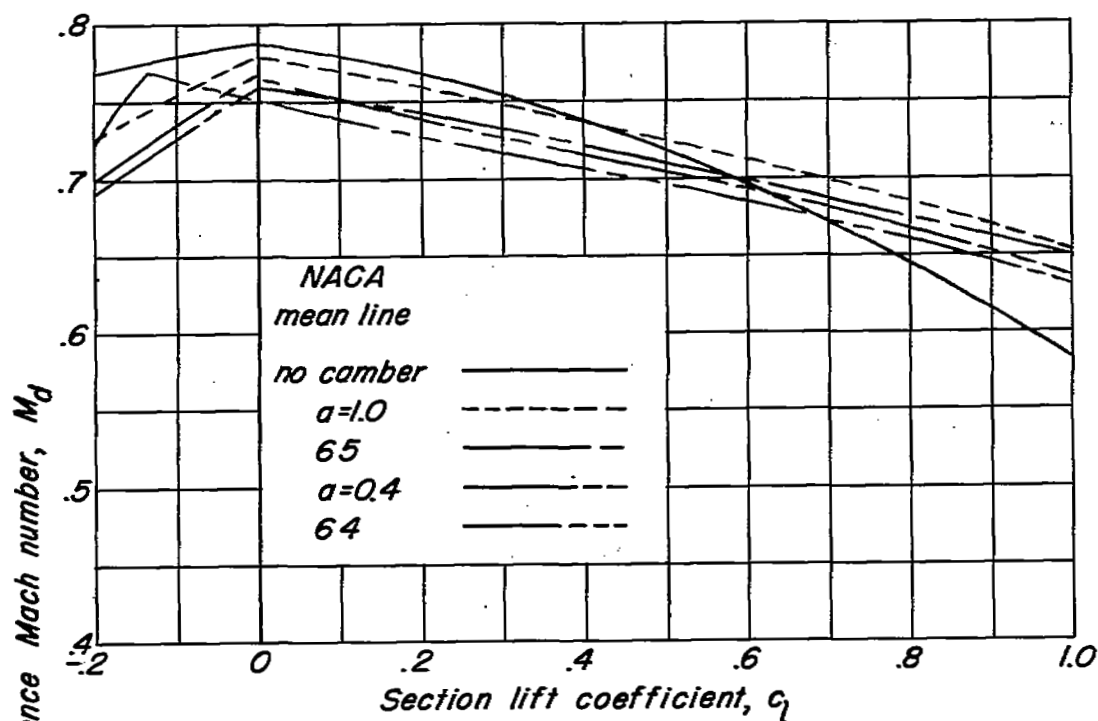
(a) Basic thickness form, NACA 64A010.
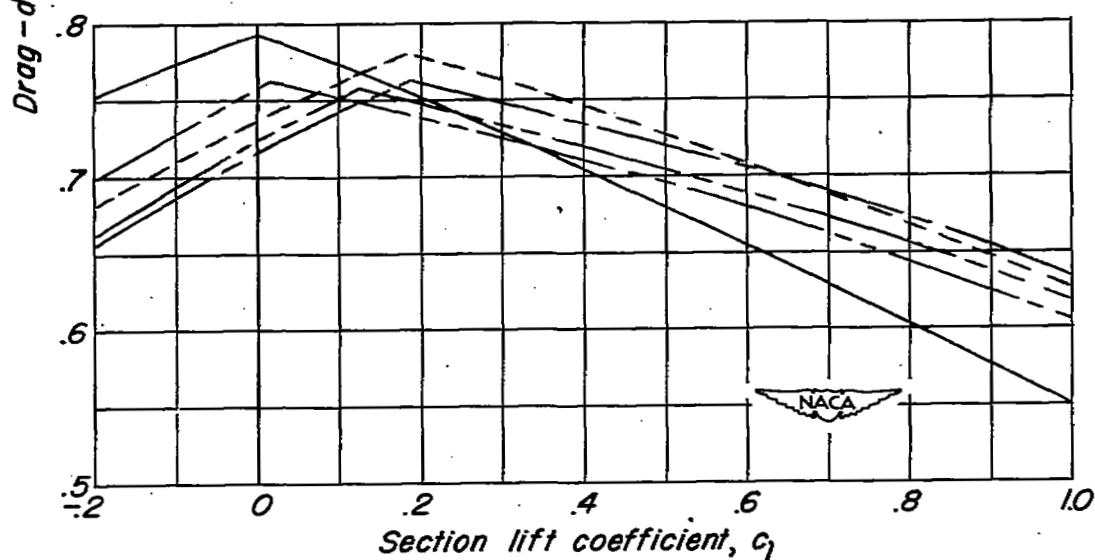
(b) Basic thickness form, NACA 0010.

Figure 3.- Effect of type of mean line on calculated variation of drag-divergence Mach number with section lift coefficient. $c_{l_i}=0.3$.
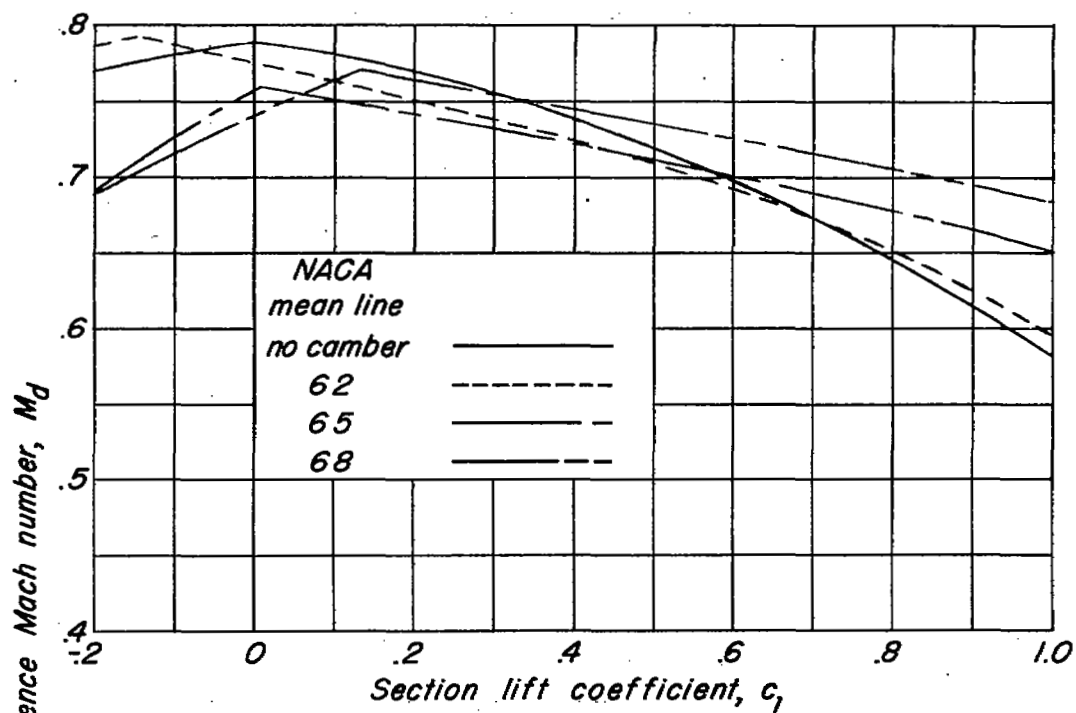
(a) Basic thickness form, NACA 64A010.
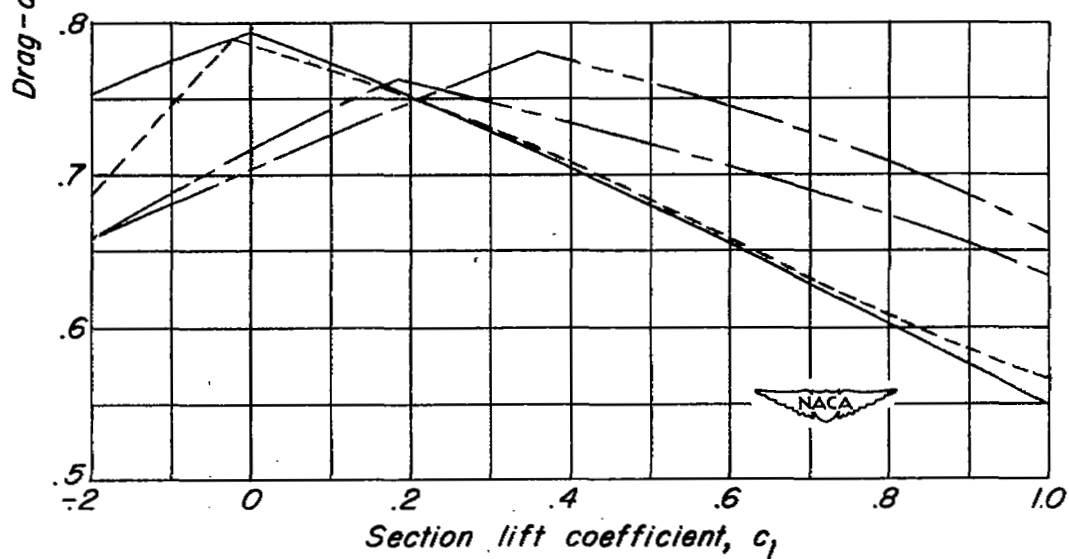
(b) Basic thickness form, NACA 0010.

Figure 4.- Effect of chordwise location of maximum camber on calculated variation of drag-divergence Mach number with section lift coefficient. $c_{l_i} = 0.3$.
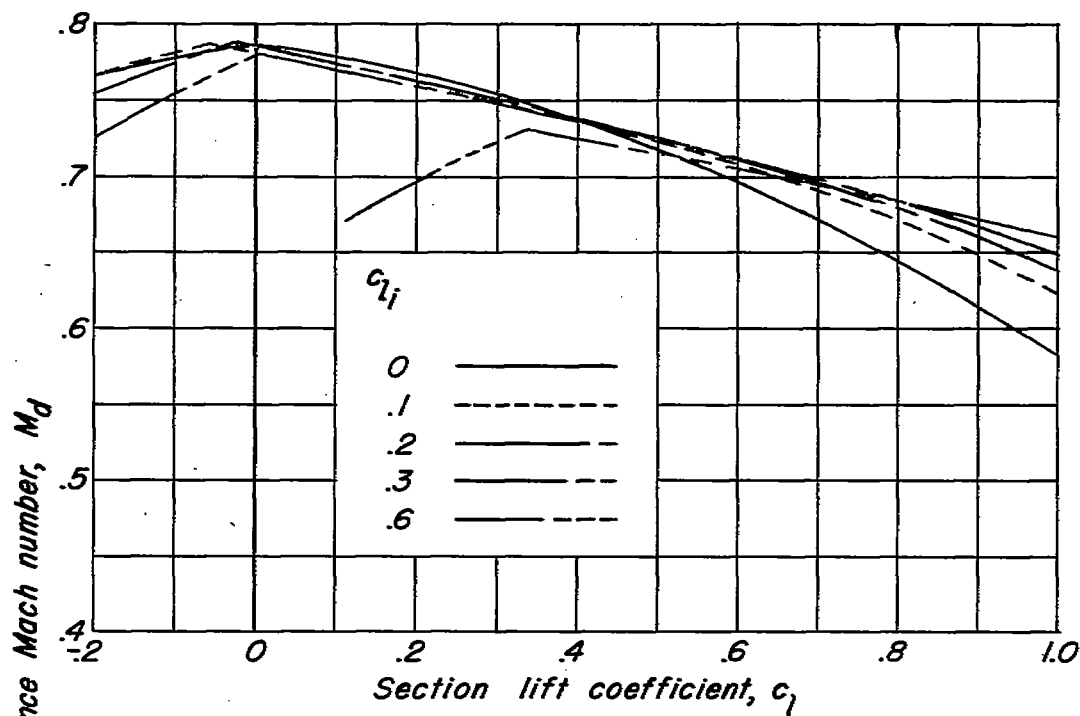
(a) Basic thickness form, NACA 64A010.
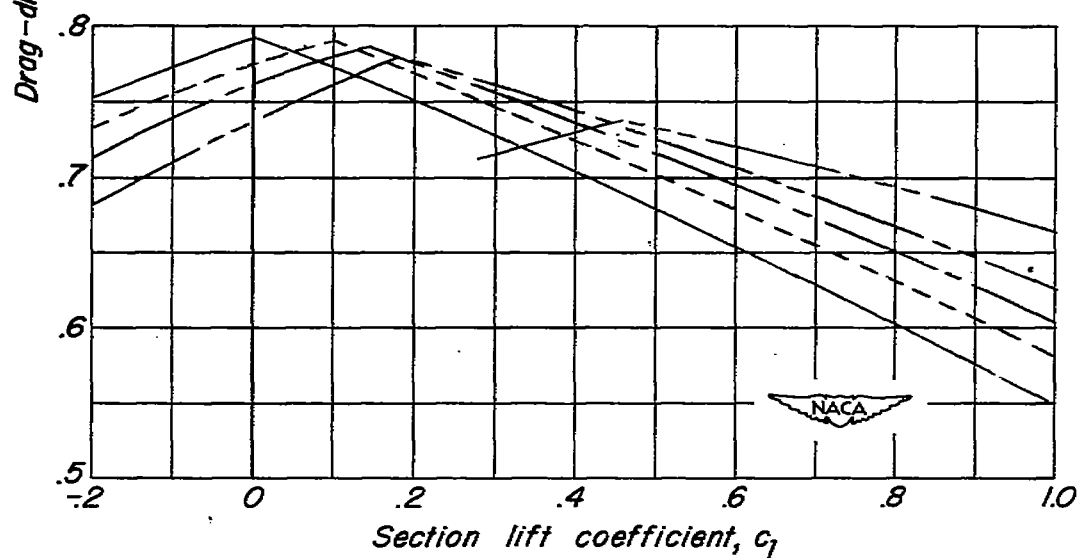
(b) Basic thickness form, NACA 0010.

Figure 5.— Effect of design lift coefficient on calculated variation of drag-
divergence Mach number with section lift coefficient for airfoil sections
with a=1.0 type mean lines.
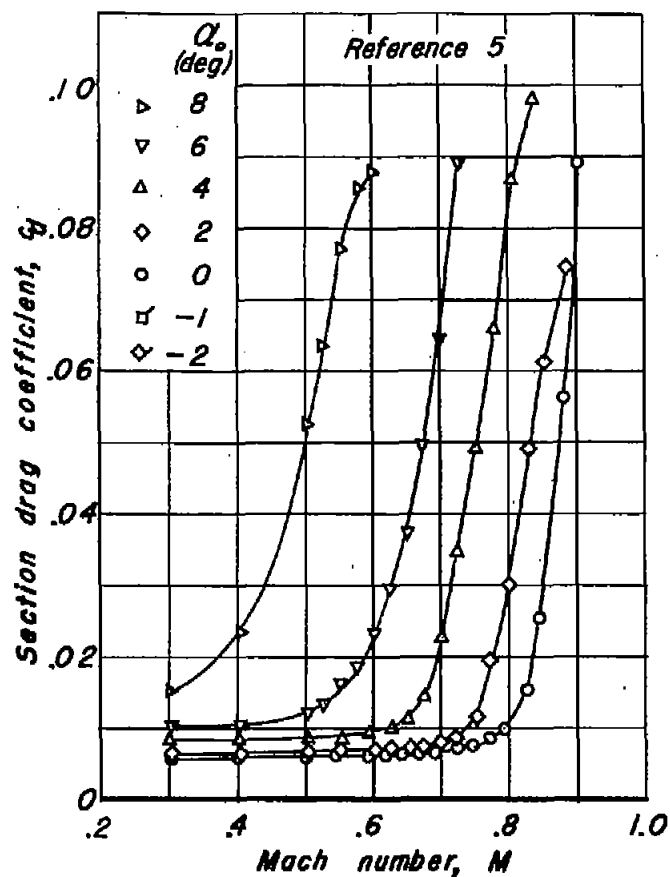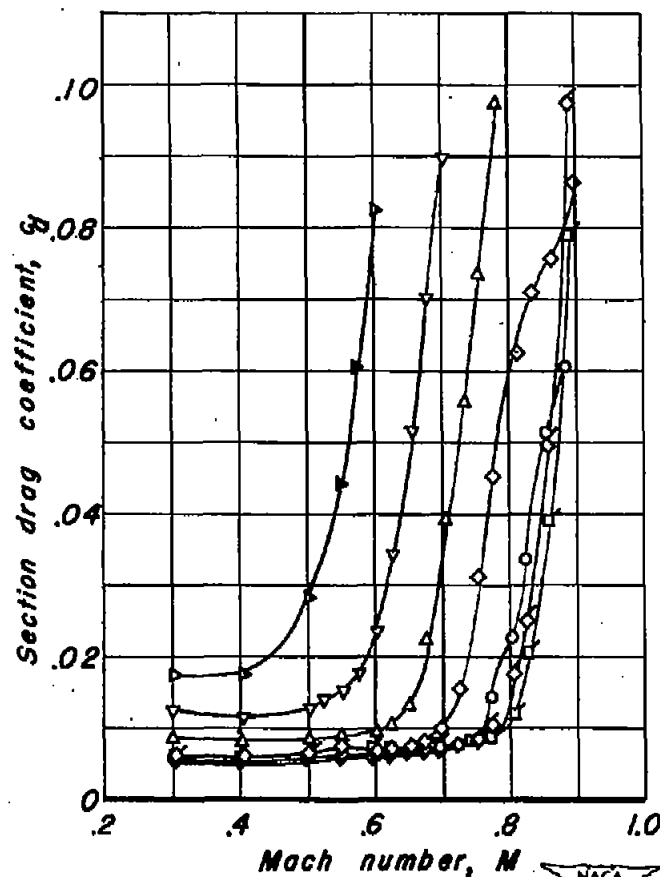
(a) Variation of section drag coefficient with Mach number.

Figure 6.— Measured variation of section force coefficients with Mach number for NACA 0010 and NACA 0010, $a=1.0$, $c_{l_i}=0.3$ airfoils.
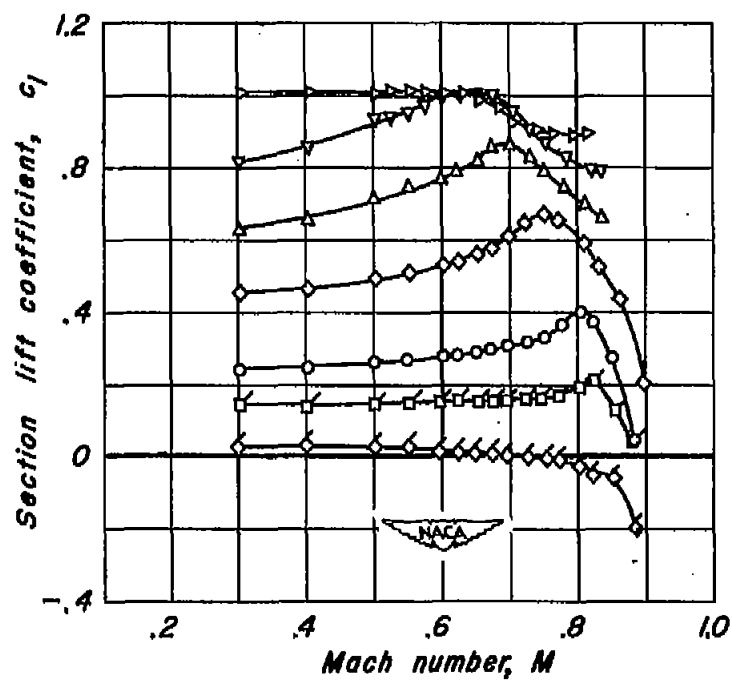
(b) Variation of section lift coefficient with Mach number,

Figure 6.—Continued.

NACA 0010

NACA 0010, $a=1.0$, $c_{l_i}=0.3$
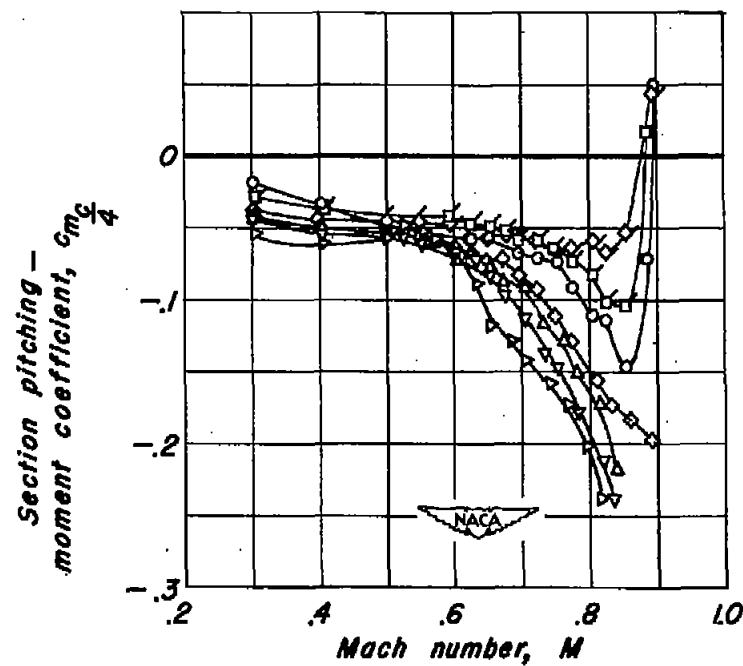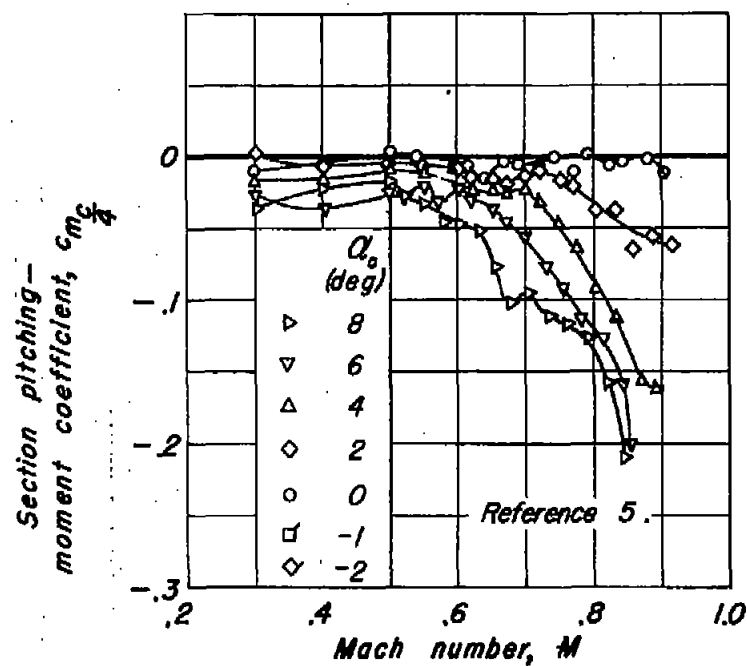
(c) Variation of section pitching - moment coefficient with Mach number.

Figure 6.— Concluded.
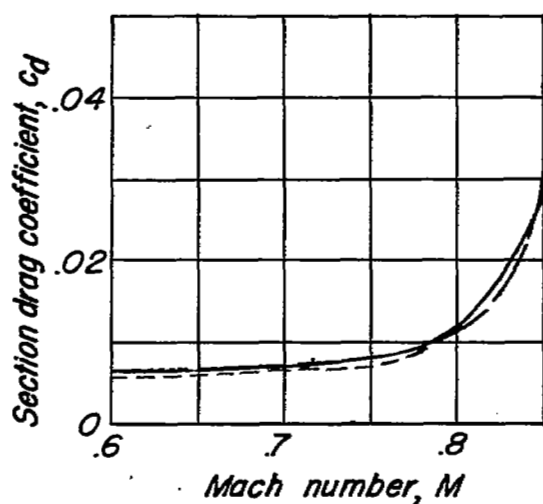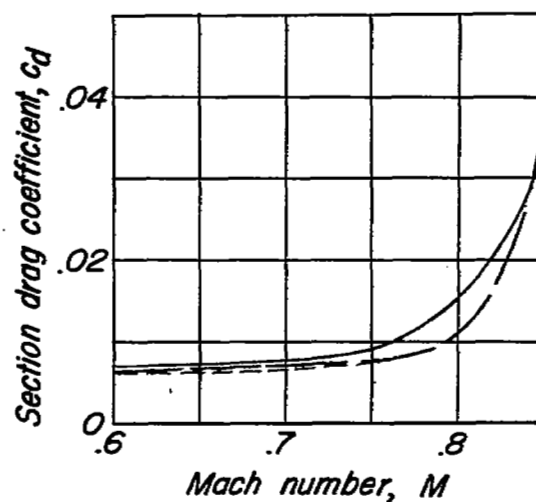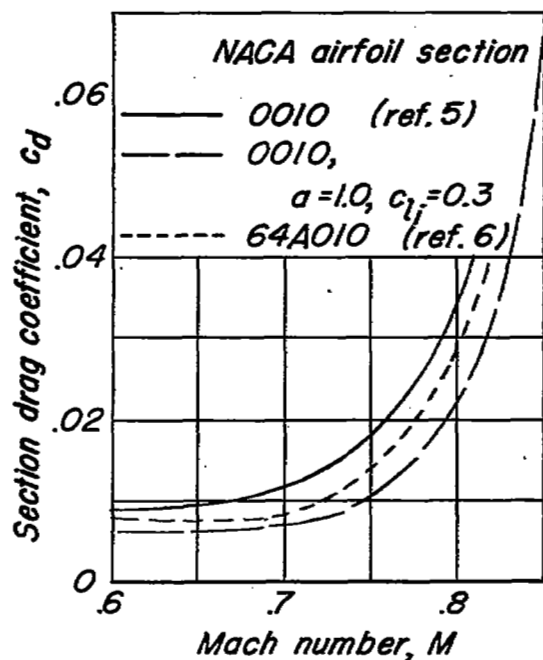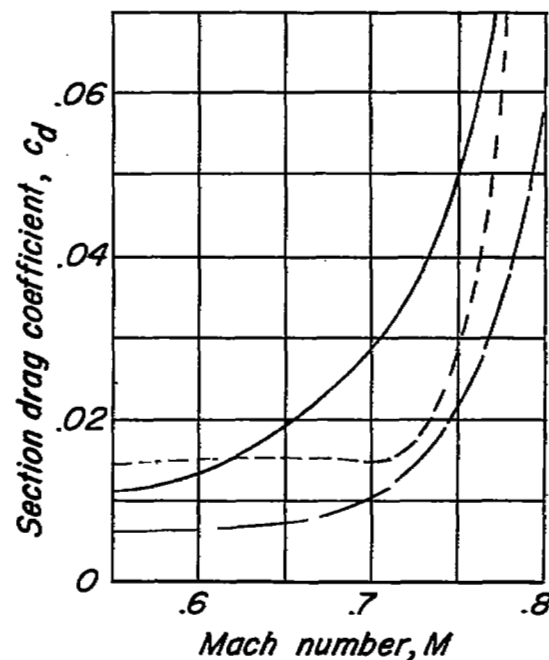
Figure 7. – Variation of section drag coefficient with Mach number at constant section lift coefficient.
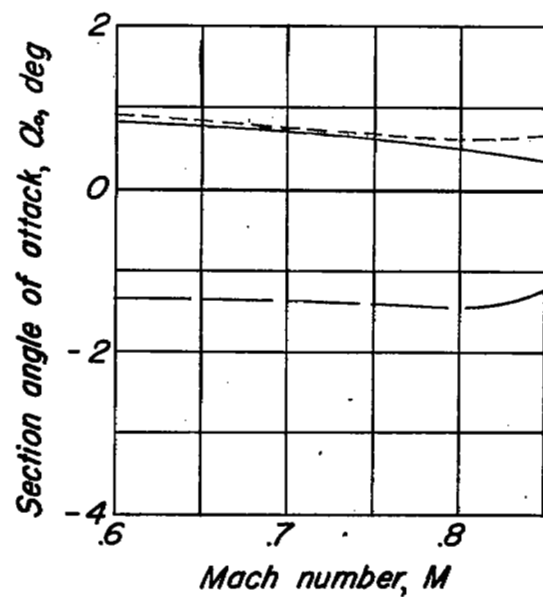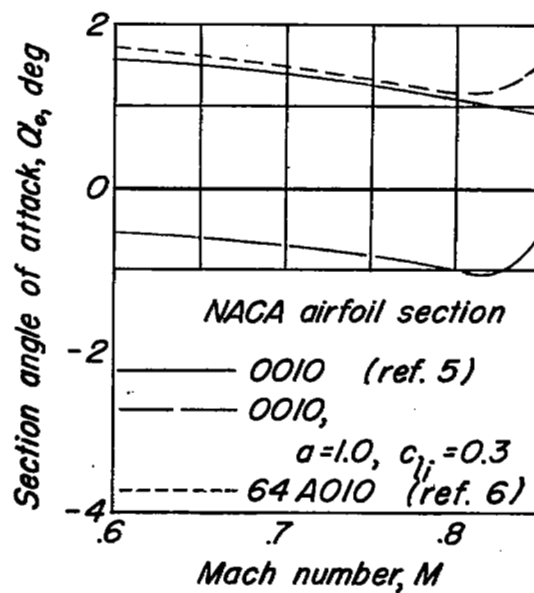
Figure 8.– Variation with Mach number of section angle of attack at
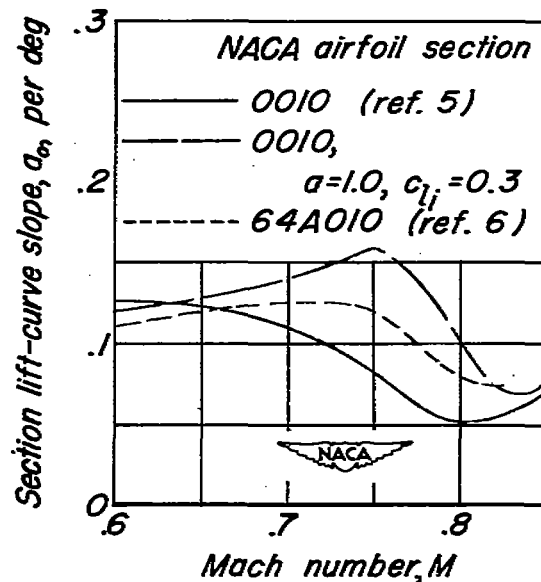constant section lift coefficient.

(a) $c_l = 0.1$.

(b) $c_l = 0.2$.

NACA airfoil section

———— OOIO (ref. 5)

— — — OOIO,

  $a=1.0$, $c_{l_i} = 0.3$

– – – – 64A0IO (ref. 6)
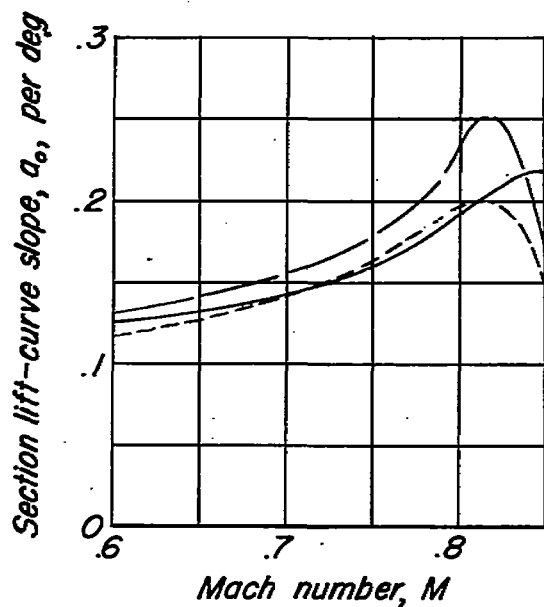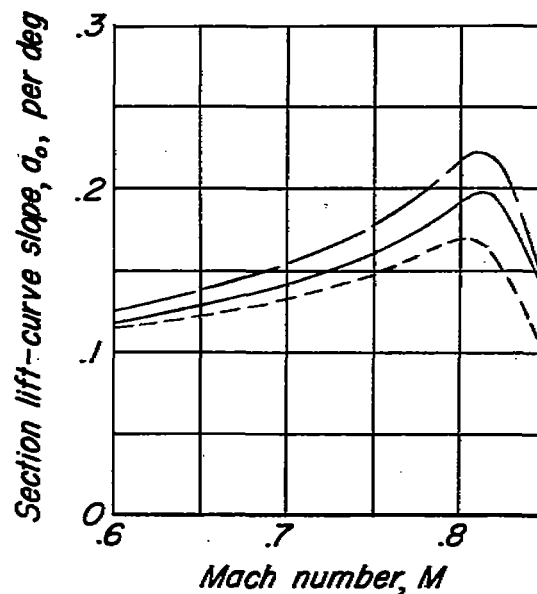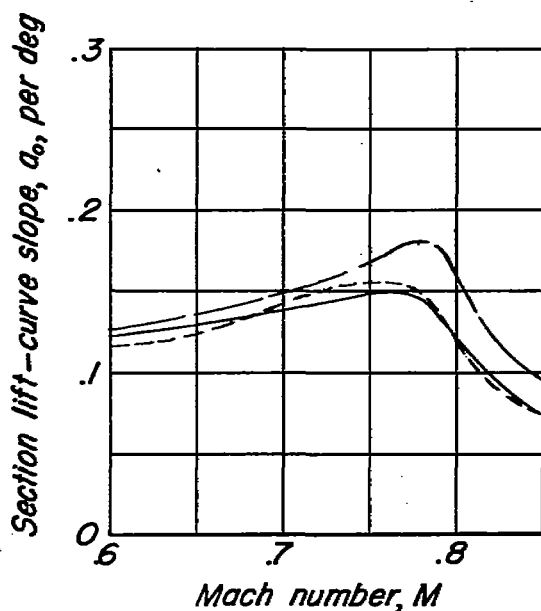
(c) $c_l = 0.4$.

(d) $c_l = 0.6$.

Figure 9.— Variation of section lift—curve slope with Mach number at constant section lift coefficient.
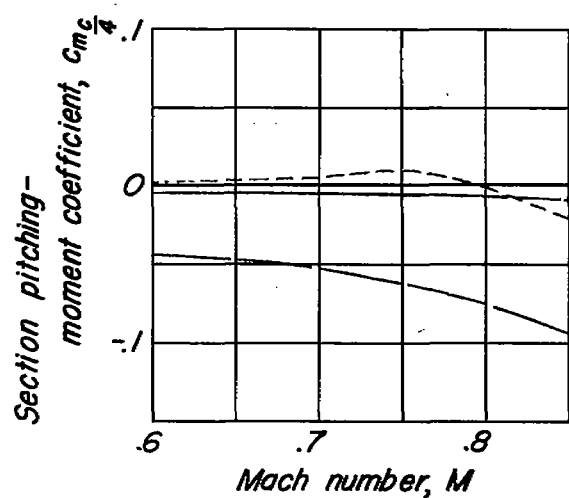
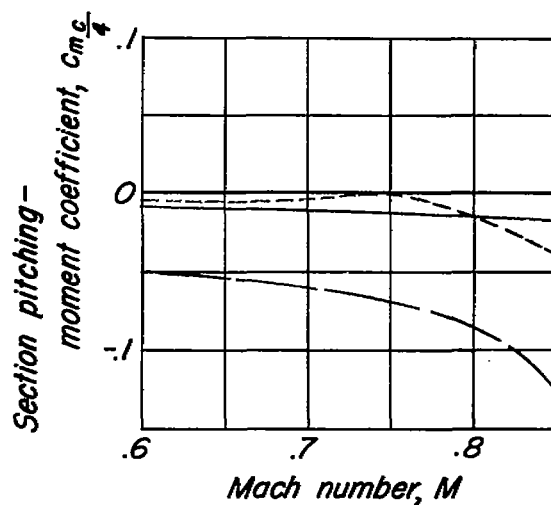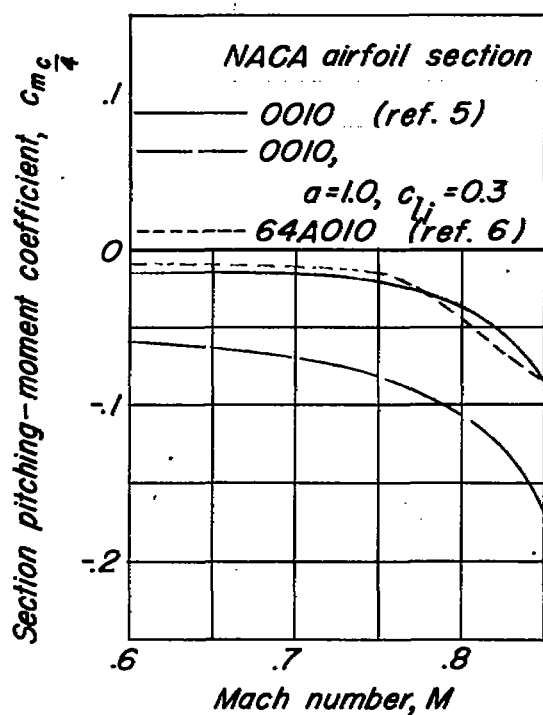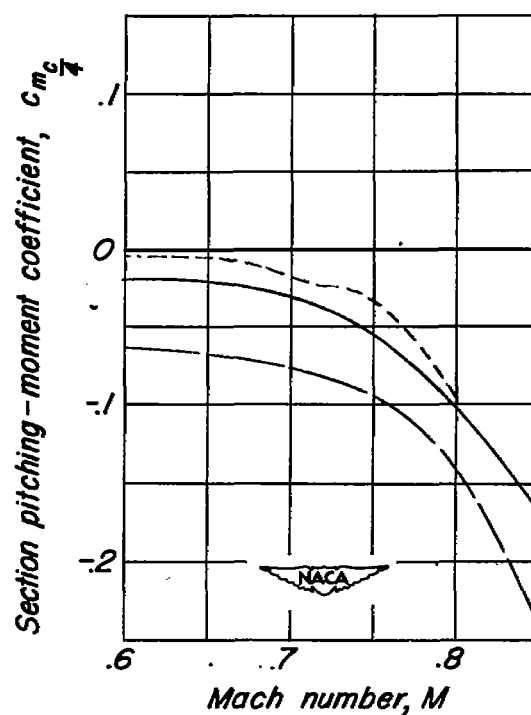Figure 10.— Variation of section pitching—moment coefficient with Mach number at constant section lift coefficient.